



HEAT TRANSFER UNDERGRADUATE COURSE

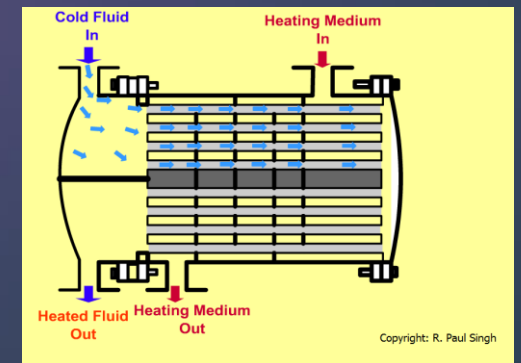
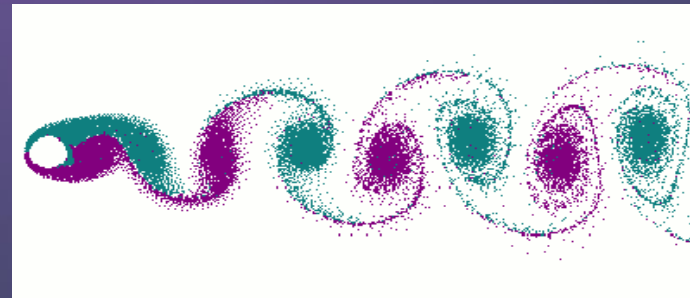
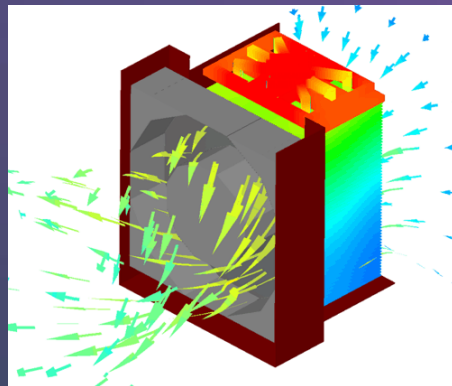
ENGINEERING & SCIENCE PLATFORM

DR. SAEED J. ALMALOWI
FALL 2016

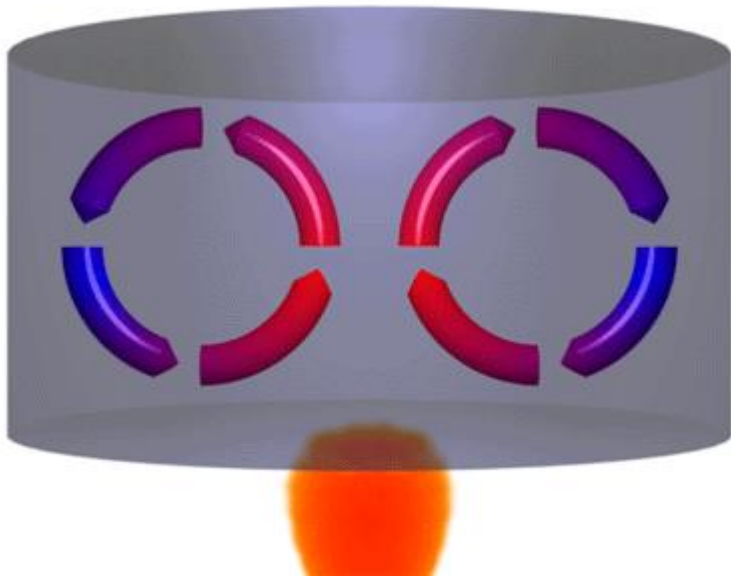
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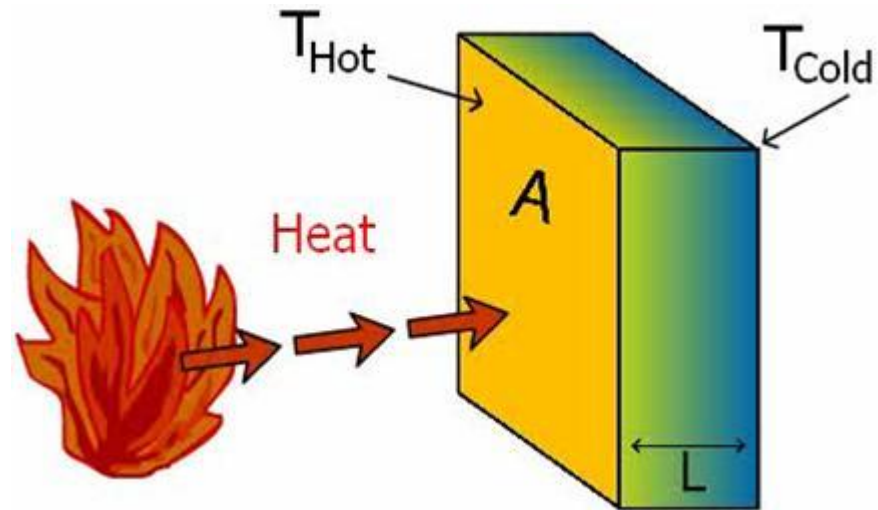
CONDUCTION



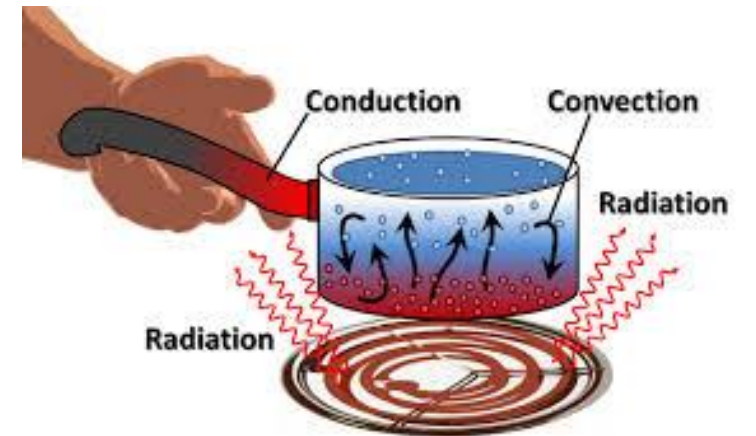
HEAT TRANSFER DEFINITIONS AND MODES



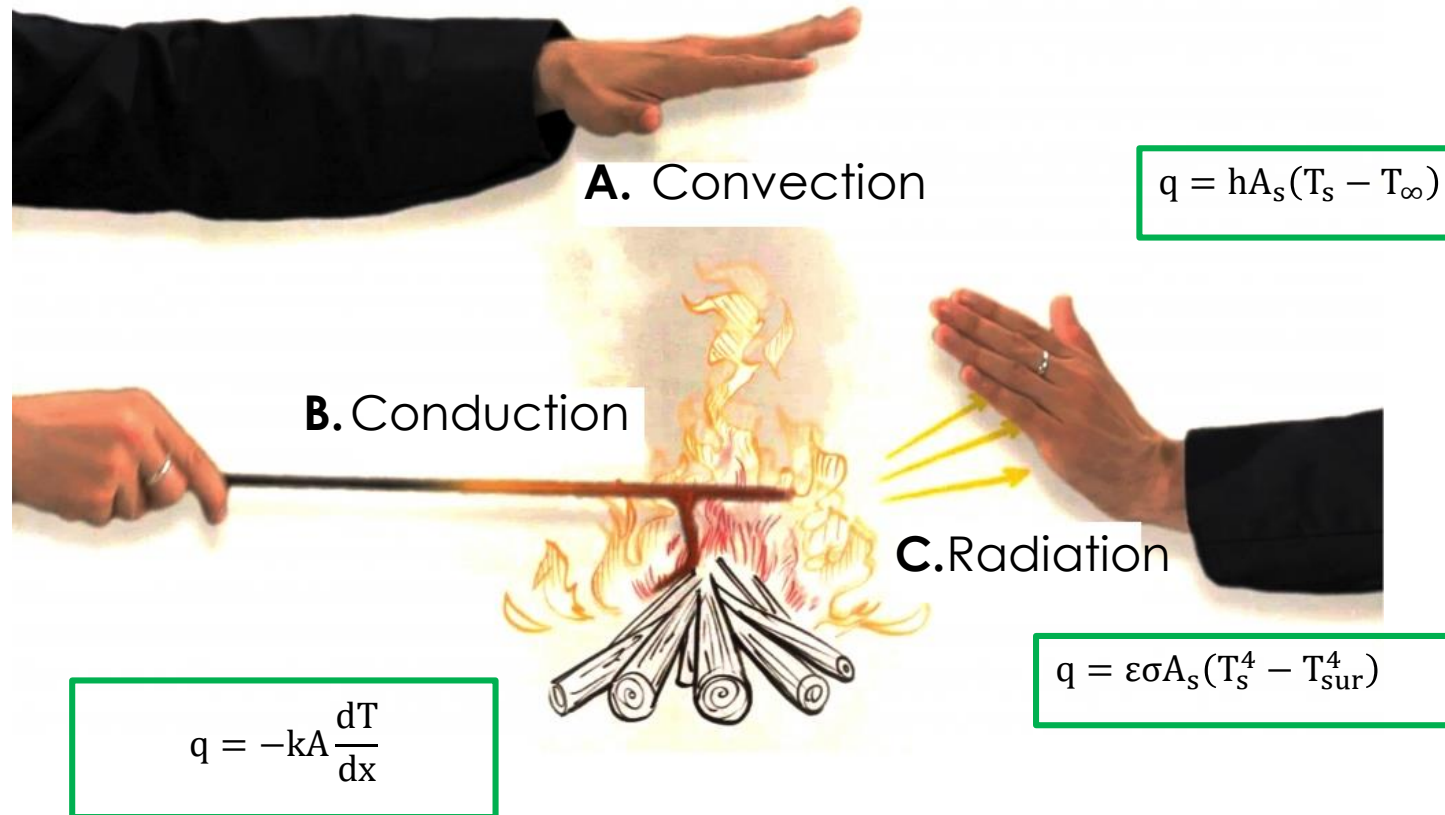
Convection Mode



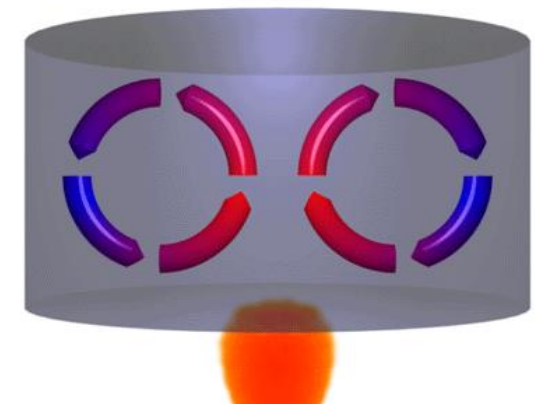
Conduction Mode



HEAT TRANSFER DEFINITIONS AND MODES



CONDUCTION



STEADY HEAT CONDUCTION IN PLANE WALLS

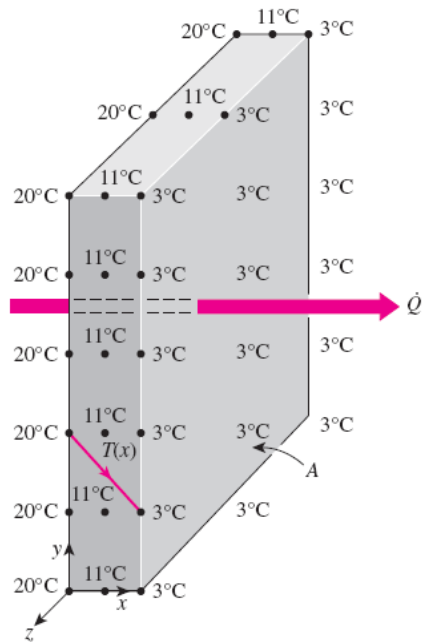


FIGURE 3-1

Heat transfer through a wall is one-dimensional when the temperature of the wall varies in one direction only.

Heat transfer through the wall of a house can be modeled as *steady and one-dimensional*.

The temperature of the wall in this case depends on one direction only (say the x -direction) and can be expressed as $T(x)$.

$$\left(\begin{array}{c} \text{Rate of} \\ \text{heat transfer} \\ \text{into the wall} \end{array} \right) - \left(\begin{array}{c} \text{Rate of} \\ \text{heat transfer} \\ \text{out of the wall} \end{array} \right) = \left(\begin{array}{c} \text{Rate of change} \\ \text{of the energy} \\ \text{of the wall} \end{array} \right)$$

$$\dot{Q}_{\text{in}} - \dot{Q}_{\text{out}} = \frac{dE_{\text{wall}}}{dt}$$

$$dE_{\text{wall}}/dt = 0$$

for *steady operation*

In steady operation, the rate of heat transfer through the wall is constant.

$$\dot{Q}_{\text{cond, wall}} = -kA \frac{dT}{dx} \quad (\text{W}) \quad \text{Fourier's law of heat conduction}$$

THERMAL RESISTANCE CONCEPT IN A PLANAR COORDINATE

$$R_{\text{wall}} = \frac{L}{kA} \quad (\text{°C/W})$$

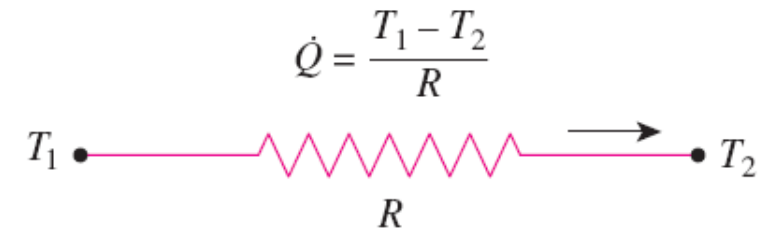
Conduction resistance of the wall:
Thermal resistance of the wall
 against heat conduction.

Thermal resistance of a medium
 depends on the *geometry* and the
thermal properties of the medium.

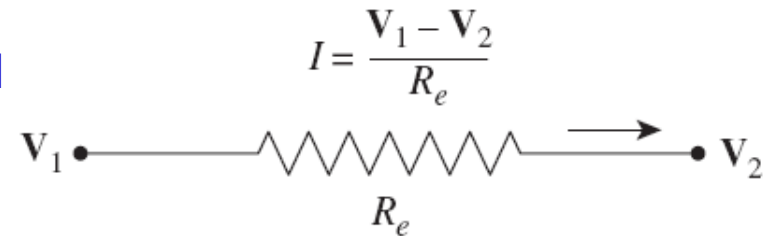
$$\dot{Q}_{\text{cond, wall}} = \frac{T_1 - T_2}{R_{\text{wall}}} \quad (\text{W})$$

$$\dot{Q}_{\text{cond, wall}} = kA \frac{T_1 - T_2}{L}$$

Analogy between thermal and electrical
 resistance concepts.



(a) Heat flow



(b) Electric current flow

$$I = \frac{V_1 - V_2}{R_e} \quad R_e = L/\sigma_e A$$

Electrical resistance

rate of heat transfer → electric current
 thermal resistance → electrical resistance
 temperature difference → voltage difference

THERMAL RESISTANCE CONCEPT IN A PLANAR COORDIANTE

$$\dot{Q}_{\text{conv}} = \frac{T_s - T_\infty}{R_{\text{conv}}} \quad (\text{W})$$

$$R_{\text{conv}} = \frac{1}{hA_s} \quad (^\circ\text{C}/\text{W})$$

Newton's law of cooling

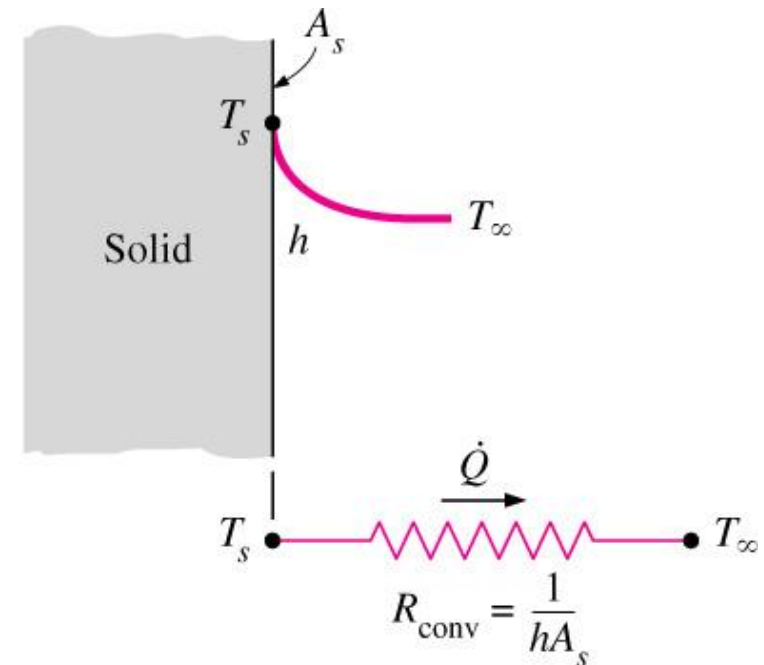
$$\dot{Q}_{\text{conv}} = hA_s (T_s - T_\infty)$$

Convection resistance of the surface: Thermal resistance of the surface against heat convection.

When the convection heat transfer coefficient is very large ($h \rightarrow \infty$), the convection resistance becomes *zero* and $T_s \approx T$.

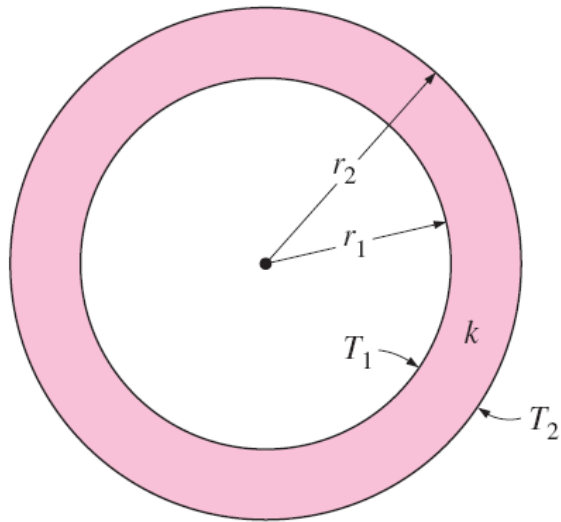
That is, the surface offers *no resistance to convection*, and thus it does not slow down the heat transfer process.

This situation is approached in practice at surfaces where boiling and condensation occur.



Schematic for convection resistance at a surface.

THERMAL RESISTANCE CONCEPT IN A SPHERICAL COORDINATE



$$\dot{Q}_{\text{cond, sph}} = \frac{T_1 - T_2}{R_{\text{sph}}}$$

A spherical shell with specified inner and outer surface temperatures T_1 and T_2 .

$$R_{\text{sph}} = \frac{r_2 - r_1}{4\pi r_1 r_2 k} = \frac{\text{Outer radius} - \text{Inner radius}}{4\pi(\text{Outer radius})(\text{Inner radius})(\text{Thermal conductivity})}$$

R_{sph} is conduction resistance of the spherical layer.

REFERENCES

1. Heat and Mass Transfer: Fundamentals & Applications Fourth Edition, Yunus A. Cengel, Afshin J. Ghajar, McGraw-Hill, 2011
2. HEAT TRANSFER (GREGORY F.NELLIS, SANFORD A.KLEIN, 2009) - BOOK